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Refinement of the Crystal Structure of Stilbite

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Stilbite, $\text{Na}_{1.28}\text{Ca}_{4.18}\text{Mg}_{0.18}[\text{Al}_{10.30}\text{Si}_{25.71}\text{O}_{72}].34.07\text{H}_2\text{O}$, a zeolite belonging to the heulandite group, crystallizes in the monoclinic, pseudo-orthorhombic, system, space group $C2/m$ with $a = 13.64$, $b = 18.24$, $c = 11.27$ Å and $\beta = 128^\circ$; $Z = 1$. The structure was refined by three-dimensional electron density syntheses and least-squares to a final reliability index R of 12.3% for observed reflexions. The silicate framework can be described as consisting of a fundamental polyhedral configuration containing four- and five-membered rings of tetrahedra. In the stilbite framework there are two sets of channels, the biggest running parallel to the a axis, the smallest to the c^* axis. Several attempts to identify the ordering of Si and Al atoms in the framework were made and the results discussed. As in related zeolites the exchangeable cations and water molecules occur within the cavities formed by the intersecting channels. Calcium atoms have been found to be completely insulated from framework atoms by a sphere of hydration of their own. Sodium atoms lie in interstices between these spheres and the framework wall. The (010) cleavage and habit of stilbite are well explained by the small number of oxygen bridges linking the tetrahedral sheets. Explanations of the twinning are suggested.

Introduction

Stilbite is a common natural zeolite formed as a result of late-stage hydrothermal activity and it occurs mainly in cavities of basalts and in crevices of metamorphic rocks.

Gabuda, Lundin & Mikhailov (1963) investigated the position of the water molecules in stilbite by the nuclear magnetic resonance method.

The description of the unrefined framework of tetrahedra of stilbite has been given by Galli & Gottardi (1966).

The purpose of this work was to refine the structure, locate the exchangeable-cation and water-molecule positions and investigate the Si/Al distribution within the framework. The results of this research, along with derived data, are given in this report.

Experimental

The stilbite studied was from a basalt from Iceland (specimen No. 3157 of the Museo di Mineralogia dell' Università di Pisa). The crystal data used in this in-

vestigation, the same as used by Galli & Gottardi (1966) are:

$$\begin{aligned} a &= 13.64 \pm 0.03 \text{ \AA}, \\ b &= 18.24 \pm 0.04 \\ c &= 11.27 \pm 0.02 \\ \beta &= 128^\circ 0' \pm 15' \\ U &= 2209 \text{ \AA}^3 \\ \text{Space group } &C2/m \end{aligned}$$

In the unit cell there is one stoichiometric unit $\text{Na}_{1.28}\text{Ca}_{4.18}\text{Mg}_{0.18}[\text{Al}_{10.30}\text{Si}_{25.71}\text{O}_{72}].34.07\text{H}_2\text{O}$

$$\begin{aligned} D_{\text{calc}} &= 2.23 \text{ g.cm}^{-3} \\ D_{\text{exp}} &= 2.19 \pm 0.01 \text{ g.cm}^{-3}. \end{aligned}$$

The experimental density was obtained with a torsion microbalance, on small splinters weighing a few milligrams.

As direction [102] is almost normal to \mathbf{a} , stilbite is pseudo-orthorhombic with unit-cell dimensions

$$a = 13.64, b = 18.24, c = 8.88 \text{ \AA}; \beta = 89^\circ 5'.$$

Photographic data were collected on a Weissenberg camera with equi-inclination geometry and on a Buer-

ger retigraph modified after Corni & Gottardi (1964). On the whole intensities of 1360 independent reflexions were obtained and measured by visual estimation using the multiple film technique. The measured reflexions comprise approximately 55% of the total number of reflexions in the Cu $K\alpha$ limiting sphere.

Refinement

The refinement was carried out by a combination of three-dimensional electron density syntheses and least-squares techniques. The starting coordinates of Si, O and Ca atoms were those of Galli & Gottardi (1966) which gave a discrepancy index value of 19%. First Na atom and water molecule positions were found by means of two successive three-dimensional electron density syntheses and electron density difference syntheses.

The refinement was then continued on an IMB 7094 computer employing the *ORFLS* program by Busing, Martin & Levy (1962). In the initial stage of the refinement, the atomic scattering factors used in the calculations of structure factors were those for neutral atoms taken from *International Tables for X-ray Crystallography* (1962).

As the temperature factors of some Si atoms using the atomic scattering factors for neutral atoms persisted in being negative during the first cycles of least-squares, in further calculations it was advisable to use the atomic scattering factors for half-ionized atoms.

After the introduction of water molecules and Na atoms the reliability index reduced to 14%. Further refinement cycles reduced the *R* value for observed reflexions to a final value of 12.3%.

The final positional and thermal parameters with their standard deviations are given in Table 1. The ob-

served and calculated structure factors are listed in Table 2.

By the atomic coordinates obtained from the last cycle of the least squares, a three-dimensional electron density difference synthesis was computed in order to locate further sites containing exchangeable cations or water molecules.

Two sites were located, both only statistically occupied probably by water molecules: the first with an occupancy of 13% the second with an occupancy of 6%. However all attempts to refine these positions by the least-squares method failed. Although the assignment of electron density to these two positions led to a reduction of the *R* value, and the interatomic distances with neighbours were rather regular, both the sites were neglected since the temperature factors were noticeably higher than the others ($B=20 \text{ \AA}^2$ or more).

The crystallochemical results obtained at the end of the refinement are in good agreement with the data of the chemical analysis.

Refinement revealed 29.40 water molecules as against the 34.07 water molecules revealed by chemical analysis; this agreement is quite satisfactory owing to the difficulty in locating the water molecules in the crystal structure of the zeolites. The refinement gave a total of 5.76 exchangeable cations; this value agrees satisfactorily with that of 5.64 indicated by the chemical analysis.

The silicate framework

A general description of the framework of stilbite has been given by Galli & Gottardi (1966). The fundamental unit of this framework can be considered the characteristic polyhedral configuration of tetrahedra which occurs also in related zeolites of the heulandite

Table 1. *Final atomic parameters with their standard deviations*

	Number of atoms in unit cell	<i>x/a</i>	<i>y/b</i>	<i>z/c</i>	<i>B</i> (\AA^2)	Occupancy observed
Si(1)	8	0.4830 ± 0.0003	0.3042 ± 0.0002	0.2420 ± 0.0004	0.46 ± 0.06	1.00
Si(2)	8	0.2653 ± 0.0003	0.3097 ± 0.0002	0.2619 ± 0.0004	0.33 ± 0.06	1.00
Si(3)	8	0.1892 ± 0.0004	0.0893 ± 0.0002	0.4846 ± 0.0004	0.40 ± 0.06	1.00
Si(4)	8	0.1124 ± 0.0003	0.3166 ± 0.0002	0.5013 ± 0.0004	0.43 ± 0.06	1.00
Si(5)	4	0.0000 ± 0.0000	0.2610 ± 0.0003	0.0000 ± 0.0000	0.42 ± 0.08	1.00
O(1)	8	0.4645 ± 0.0010	0.2911 ± 0.0006	0.0842 ± 0.0011	1.40 ± 0.17	1.00
O(2)	8	0.1164 ± 0.0010	0.3162 ± 0.0006	0.1189 ± 0.0011	1.38 ± 0.17	1.00
O(3)	8	0.0512 ± 0.0011	0.2661 ± 0.0006	0.3516 ± 0.0012	2.03 ± 0.20	1.00
O(4)	8	0.0638 ± 0.0010	0.1199 ± 0.0006	0.3226 ± 0.0011	1.41 ± 0.18	1.00
O(5)	8	0.2935 ± 0.0011	0.2308 ± 0.0006	0.3453 ± 0.0012	2.01 ± 0.20	1.00
O(6)	8	0.3001 ± 0.0011	0.3796 ± 0.0006	0.3714 ± 0.0012	1.76 ± 0.19	1.00
O(7)	8	0.3406 ± 0.0010	0.3162 ± 0.0006	0.1914 ± 0.0011	1.40 ± 0.18	1.00
O(8)	8	0.3157 ± 0.0011	0.1119 ± 0.0006	0.5024 ± 0.0012	1.78 ± 0.19	1.00
O(9)	4	0.1863 ± 0.0016	0.0000 ± 0.0000	0.4876 ± 0.0017	1.75 ± 0.27	1.00
O(10)	4	0.0000 ± 0.0000	0.3509 ± 0.0008	0.5000 ± 0.0000	1.15 ± 0.23	1.00
Ca	4	0.2805 ± 0.0005	0.0000 ± 0.0000	0.0949 ± 0.0006	2.15 ± 0.09	1.00
Na	8	0.5055 ± 0.0043	0.0659 ± 0.0021	0.0392 ± 0.0042	4.28 ± 1.29	0.22 ± 0.03
H ₂ O(1)	8	0.1347 ± 0.0025	0.0776 ± 0.0015	0.1067 ± 0.0030	7.45 ± 0.98	0.84 ± 0.06
H ₂ O(2)	8	0.3306 ± 0.0018	0.1258 ± 0.0018	0.1013 ± 0.0020	4.71 ± 0.58	0.91 ± 0.05
H ₂ O(3)	4	0.3691 ± 0.0024	0.0000 ± 0.0000	0.3549 ± 0.0027	3.58 ± 0.71	0.85 ± 0.06
H ₂ O(4)	4	0.5124 ± 0.0038	0.0000 ± 0.0000	0.2416 ± 0.0045	9.98 ± 1.06	1.00
H ₂ O(5)	4	0.4028 ± 0.0023	0.5000 ± 0.0000	0.1632 ± 0.0026	4.72 ± 0.51	1.00
H ₂ O(6)	4	0.1712 ± 0.0039	0.5000 ± 0.0000	0.1040 ± 0.0046	10.16 ± 1.07	1.00

Table 2. Observed and calculated structure factors (x 10)

K	L	FO	FC	K	L	FO	FC	K	L	FO	FC	K	L	FO	FC	K	L	FO	FC	K	L	FO	FC	K	L	FO	FC																																																																																																																																																																																																																																																																																																																																																																																								
0	0	0	0	1	1	1	1	2	2	2	2	3	3	3	3	4	4	4	4	5	5	5	5	6	6	6	6	7	7	7	7	8	8	8	8	9	9	9	9	10	10	10	10	11	11	11	11	12	12	12	12	13	13	13	13	14	14	14	14	15	15	15	15	16	16	16	16	17	17	17	17	18	18	18	18	19	19	19	19	20	20	20	20	21	21	21	21	22	22	22	22	23	23	23	23	24	24	24	24	25	25	25	25	26	26	26	26	27	27	27	27	28	28	28	28	29	29	29	29	30	30	30	30	31	31	31	31	32	32	32	32	33	33	33	33	34	34	34	34	35	35	35	35	36	36	36	36	37	37	37	37	38	38	38	38	39	39	39	39	40	40	40	40	41	41	41	41	42	42	42	42	43	43	43	43	44	44	44	44	45	45	45	45	46	46	46	46	47	47	47	47	48	48	48	48	49	49	49	49	50	50	50	50	51	51	51	51	52	52	52	52	53	53	53	53	54	54	54	54	55	55	55	55	56	56	56	56	57	57	57	57	58	58	58	58	59	59	59	59	60	60	60	60	61	61	61	61	62	62	62	62	63	63	63	63	64	64	64	64	65	65	65	65	66	66	66	66	67	67	67	67	68	68	68	68	69	69	69	69	70	70	70	70	71	71	71	71	72	72	72	72	73	73	73	73	74	74	74	74	75	75	75	75	76	76	76	76	77	77	77	77	78	78	78	78	79	79	79	79	80	80	80	80	81	81	81	81	82	82	82	82	83	83	83	83	84	84	84	84	85	85	85	85	86	86	86	86	87	87	87	87	88	88	88	88	89	89	89	89	90	90	90	90	91	91	91	91	92	92	92	92	93	93	93	93	94	94	94	94	95	95	95	95	96	96	96	96	97	97	97	97	98	98	98	98	99	99	99	99	100	100	100	100

group and consists of four- and five-membered rings of tetrahedra (Meier, 1968). The units are connected with each other giving rise to elongated chains in the same direction as c^* and to sheets parallel to (010). The sheets are linked together by relatively few oxygen-bridges which occur at $y/b=0$ and $y/b=\frac{1}{2}$.

Two dimensional systems of channels are therefore formed. The intersecting channels are relatively large; ten-membered rings surround those channels running

parallel to the a axis and eight-membered rings surround those running parallel to the c axis. All the channels are bisected by the mirror plane at heights of 0 and $\frac{1}{2}$ on the crystallographic b axis and are limited by a complex layer arrangement of six-, five- and four-membered ring groups. The stereographic views of Fig. 1 (a) and (b) show the silicate framework as seen along the a axis and [102] axis. The (Si, Al)—O bond length and bond angles are presented in Tables 3 and 4, as well as

Table 3. *Interatomic distances with their standard errors within the framework*

Interatomic distances symmetrically equivalent are bracketed.

Distances		Distances	
Si(1) tetrahedron		Si(3) tetrahedron	
Si(1)—O(1)	1.65 ± 0.01 Å	Si(3)—O(4)	1.65 ± 0.01 Å
Si(1)—O(3 ⁱⁱⁱ)	1.62 ± 0.01	Si(3)—O(6 ^{vi})	1.64 ± 0.01
Si(1)—O(4 ⁱⁱⁱ)	1.65 ± 0.01	Si(3)—O(8)	1.66 ± 0.01
Si(1)—O(7)	1.67 ± 0.01	Si(3)—O(9)	1.63 ± 0.01
Average	1.64	Average	1.64
O(1)—O(3 ⁱⁱⁱ)	2.68 ± 0.02	O(4)—O(6 ^{vi})	2.73 ± 0.02
O(1)—O(4 ⁱⁱⁱ)	2.68 ± 0.02	O(4)—O(8)	2.71 ± 0.02
O(1)—O(7)	2.65 ± 0.02	O(4)—O(9)	2.69 ± 0.01
O(3)—O(4)	2.70 ± 0.02	O(6 ^{vi})—O(8)	2.70 ± 0.02
O(3 ⁱⁱⁱ)—O(7)	2.72 ± 0.02	O(6 ^{vi})—O(9)	2.65 ± 0.01
O(4 ⁱⁱⁱ)—O(7)	2.70 ± 0.02	O(8)—O(9)	2.64 ± 0.02
Si(2) tetrahedron		Si(4) tetrahedron	
Si(2)—O(2)	1.65 ± 0.01	Si(4)—O(3)	1.63 ± 0.01
Si(2)—O(5)	1.63 ± 0.01	Si(4)—O(5 ^{vi})	1.63 ± 0.01
Si(2)—O(6)	1.63 ± 0.01	Si(4)—O(8 ^{vi})	1.65 ± 0.01
Si(2)—O(7)	1.64 ± 0.01	Si(4)—O(10)	1.65 ± 0.01
Average	1.63	Average	1.64
O(2)—O(5)	2.68 ± 0.02	O(3)—O(5 ^{vi})	2.69 ± 0.02
O(2)—O(6)	2.63 ± 0.02	O(3)—O(8 ^{vi})	2.70 ± 0.02
O(2)—O(7)	2.64 ± 0.02	O(3)—O(10)	2.67 ± 0.01
O(5)—O(6)	2.73 ± 0.02	O(5)—O(8)	2.70 ± 0.02
O(5)—O(7)	2.69 ± 0.02	O(5 ^{vi})—O(10)	2.67 ± 0.02
O(6)—O(7)	2.67 ± 0.02	O(8 ^{vi})—O(10)	2.62 ± 0.01
Si(5) tetrahedron			
Si(5)—O(1 ^{iv})	1.61 ± 0.01 Å		
Si(5)—O(1 ^v)			
Si(5)—O(2)	1.65 ± 0.01		
Si(5)—O(2 ⁱ)			
Average	1.63		
O(1 ^{iv})—O(1 ^v)	2.61 ± 0.02		
O(1 ^{iv})—O(2)	2.70 ± 0.02		
O(1 ^v)—O(2 ⁱ)			
O(1 ^{iv})—O(2 ⁱ)	2.68 ± 0.02		
O(1 ^v)—O(2)			
O(2)—O(2 ⁱ)	2.60 ± 0.02		

The atoms of the different asymmetric units are related to the atoms of the fundamental unit as follows:

Superscript	Coordinates		
none	x	y	z
i	$-x$	y	$-z$
ii	$1-x$	$-y$	$-z$
iii	$\frac{1}{2}+x$	$\frac{1}{2}+y$	z
iv	$x-\frac{1}{2}$	$\frac{1}{2}-y$	z
v	$\frac{1}{2}-x$	$\frac{1}{2}-y$	$-z$
vi	$\frac{1}{2}-x$	$\frac{1}{2}-y$	$1-z$
vii	x	$-y$	z
viii	$1-x$	y	$1-z$
ix	$\frac{1}{2}-x$	$\frac{1}{2}+y$	$-z$

This also applies in Tables 4 and 5 and Fig. 2.

their standard errors. The whole structural model of stilbite projected on (010) plane is shown in Fig. 2. The average value of 1.64 Å for all (Si, Al)–O distances is the same as that expected for Si, Al ratio of 25.7/10.3.

Discussion of the structure

1. Order–disorder of Al, Si atoms

Single-crystal Weissenberg and precession photographs of stilbite show monoclinic symmetry with extinctions hkl , $h+k=2n+1$ which is consistent with the space groups $C2/m$, Cm or $C2$.

Although stilbite was refined with the centrosymmetric space group the Si/Al arrangement in the framework may have lower symmetry. In fact only if the Si and Al atoms are completely disordered will the symmetry be centrosymmetric, but only on a statistical basis. However, the problem of the Si/Al distribution in zeolites is far too involved to be easily resolved.

The only reliable method of determining the occupancy of the tetrahedral sites by Si or Al is based on the length of the interatomic distances which differ by no more than about 0.13 Å.

The stilbite refinement in space group $C2/m$ gave distances equal within experimental error in all framework tetrahedra.

The calcium site, which should be closely associated with aluminum-substituted tetrahedra to minimize the Coulomb energy, did not help solve the problem, since this atom is near the middle of the channels and completely surrounded by eight water molecules and not by framework oxygen atoms. After the last centrosymmetric refinement, a careful inspection of the three-

dimensional electron density map did not reveal any evidence of departure from mirror symmetry, as the peaks of the atoms at $y/b=\frac{1}{2}$ did not exhibit significant deviations from sphericity.

However, several attempts to refine the crystal structure of stilbite were made using both the non-centrosymmetric space groups $C2$ and Cm . Twelve different models have been tested, each obtained by placing aluminum into two or three sites according to the rule 'two aluminum tetrahedra cannot be directly linked'.

The passage from $C2/m$ to Cm or $C2$ was obtained by splitting up the atoms, which in the centrosymmetric space group are single, into double in the non-centrosymmetric space group, excluding, of course, the atoms not splitting for reasons of symmetry.

The data obtained from the different trials in non-centrosymmetric space groups show that:

(a) It is impossible to draw conclusions on the reliability of the different models because the R values for all postulated models reached equal values, which in turn were just a little smaller than the value obtained for space group $C2/m$;

(b) The (Si, Al)–O distances within each tetrahedron show a range of values too large to be reliable;

(c) If the average distances within each tetrahedron of the two structural models proposed for space group Cm give insufficient evidence, the average values (Si, Al)–O for all ten suggested models for space group $C2$ show similarities in preferential occupation by aluminum.

Those similarities can be summarized as follows:

(d) Any presence of aluminum in the Si(4) tetrahedron seems to be rejected; this agrees with the

Table 4. Bond angles with their standard errors within the framework

Bond angles symmetrically equivalent are bracketed.			
Si(1) tetrahedron	Bond angle	Si(4) tetrahedron	Bond angle
O(1)—Si(1)—O(3 ⁱⁱⁱ)	109.96 ± 0.59°	O(3)—Si(4)—O(5 ^{vi})	111.44 ± 0.62°
O(1)—Si(1)—O(4 ⁱⁱⁱ)	108.73 ± 0.56	O(3)—Si(4)—O(8 ^{vi})	110.72 ± 0.60
O(1)—Si(1)—O(7)	106.09 ± 0.58	O(3)—Si(4)—O(10)	108.95 ± 0.56
O(3 ⁱⁱⁱ)—Si(1)—O(4 ⁱⁱⁱ)	111.66 ± 0.60	O(5 ^{vi})—Si(4)—O(8 ^{vi})	110.75 ± 0.63
O(3 ⁱⁱⁱ)—Si(1)—O(7)	111.50 ± 0.60	O(5 ^{vi})—Si(4)—O(10)	109.44 ± 0.54
O(4 ⁱⁱⁱ)—Si(1)—O(7)	108.72 ± 0.58	O(8 ^{vi})—Si(4)—O(10)	105.35 ± 0.66
Average	109.44	Average	109.44
Si(2) tetrahedron	Bond angle	Si(5) tetrahedron	Bond angle
O(2)—Si(2)—O(5)	109.83 ± 0.58	O(1 ^{iv})—Si(5)—O(1 ^v)	107.80 ± 0.79
O(2)—Si(2)—O(6)	107.04 ± 0.59	O(1 ^{iv})—Si(5)—O(2)	} 111.69 ± 0.52
O(2)—Si(2)—O(7)	106.47 ± 0.59	O(1 ^v)—Si(5)—O(2 ⁱ)	
O(5)—Si(2)—O(6)	113.51 ± 0.60	O(1 ^{iv})—Si(5)—O(2 ⁱ)	
O(5)—Si(2)—O(7)	110.35 ± 0.59	O(1 ^v)—Si(5)—O(2)	
O(6)—Si(2)—O(7)	109.35 ± 0.60	O(2)—Si(5)—O(2 ⁱ)	104.55 ± 0.80
Average	109.42	Average	109.48
Si(3) tetrahedron	Bond angle	Si(1)—O(7)—Si(2)	140.11 ± 0.69
O(4)—Si(3)—O(6 ^{vi})	112.24 ± 0.60	Si(1 ^{iv})—O(4)—Si(3)	141.12 ± 0.67
O(4)—Si(3)—O(8)	109.97 ± 0.59	Si(1 ^{iv})—O(3)—Si(4)	157.59 ± 0.80
O(4)—Si(3)—O(9)	109.79 ± 0.74	Si(1 ^{iv})—O(1 ^{iv})—Si(5)	144.66 ± 0.70
O(6 ^{vi})—Si(3)—O(8)	110.01 ± 0.60	Si(2)—O(6)—Si(3 ^{vi})	145.86 ± 0.77
O(6 ^{vi})—Si(3)—O(9)	108.25 ± 0.74	Si(2)—O(5)—Si(4 ^{vi})	146.38 ± 0.77
O(8)—Si(3)—O(9)	106.39 ± 0.80	Si(2)—O(2)—Si(5)	137.98 ± 0.70
Average	109.44	Si(3)—O(8)—Si(4 ^{vi})	147.51 ± 0.75
		Average	144.40

Al-O-Al avoidance rule since each Si(4) tetrahedron is connected to an equivalent one across the twofold axis at $z/c = \frac{1}{2}$.

(e) There is a large amount of evidence to show that the two independent positions obtained by splitting the Si(5) position are preferentially occupied one by aluminum, and the second by silicon respectively.

(f) Also the two positions obtained by splitting the Si(1) eightfold position of the centrosymmetric space group, although less clear than the preceding one, seems preferentially occupied, one by Al and the second by Si. The same also holds for the Si(2) and Si(3) positions but here the evidence is more uncertain.

Therefore, if the ordering really occurs in the non-centrosymmetric $C2$ space group, bearing in mind the possible Al arrangements which can be postulated in this space group according to the earlier mentioned rule, when three positions contemporaneously are occupied by aluminum atoms, in the author's opinion the pattern of Al distribution follows the scheme $T(1D)$, $T(3D)$, $T(5D)$, or its opposite $T(1U)$, $T(3U)$, $T(5U)$, where, in the $C2$ space group, $T(nD)$ and $T(nU)$ are the two groups having independent positions which correspond to one group only having equivalent positions $T(n)$ in the centrosymmetric $C2/m$ space group; $T(nD)$ are the positions with $y/b < \frac{1}{2}$ and $T(nU)$ those with $y/b > \frac{1}{2}$.

2. The water molecules and exchangeable cations

In the structural model of stilbite the exchangeable cations and water molecules have been found to occur completely inside the cavities formed at the intersection of the larger channels, which are parallel to a , with the smaller channels which are parallel to the $[102]$ direction.

The calcium atom lies nearly on the screw axis at $z/c = 0$. It is wholly surrounded by and bonded to eight water molecules.

Of these eight water molecules, four lie on the mirror (010) plane; the other four lie on a plane which is normal to the mirror plane and parallel to the larger channel axis, obviously two above and two under the mirror.

Table 5. Bond lengths from exchangeable cations to water molecules and oxygens ions of the framework

Interatomic distances symmetrically equivalent are bracketed.

Ca polyhedron	
Ca-H ₂ O(1)	} 2.51 ± 0.03 Å
Ca-H ₂ O(1 ^{vi})	
Ca-H ₂ O(2)	} 2.38 ± 0.02
Ca-H ₂ O(2 ^{vi})	
Ca-H ₂ O(3)	2.38 ± 0.03
Ca-H ₂ O(4)	2.51 ± 0.04
Ca-H ₂ O(5 ^v)	2.40 ± 0.03
Ca-H ₂ O(6 ^v)	2.70 ± 0.04

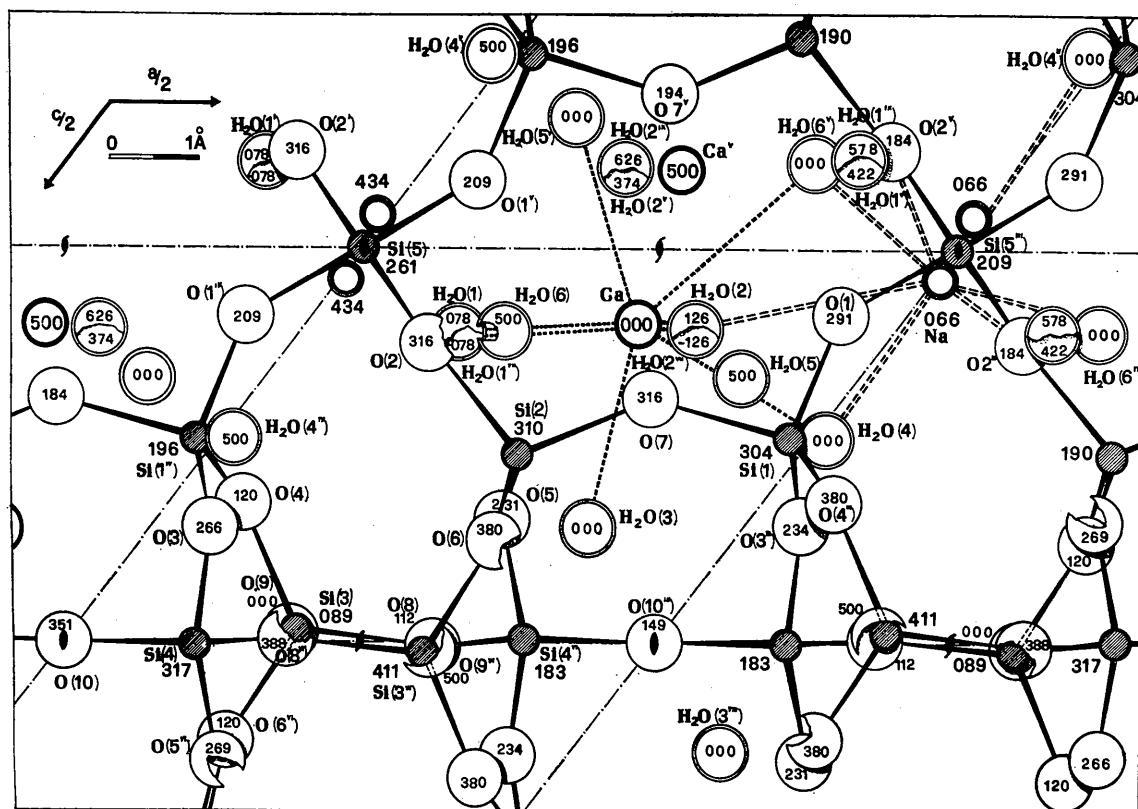
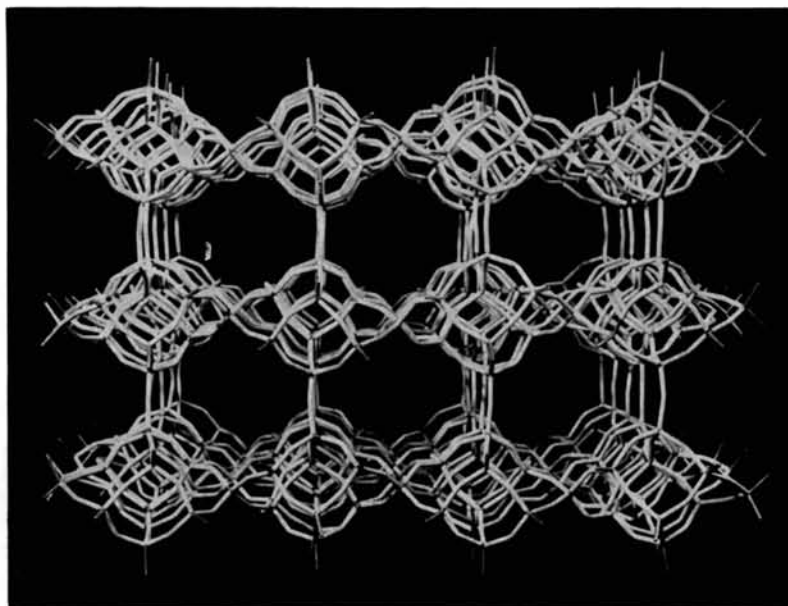
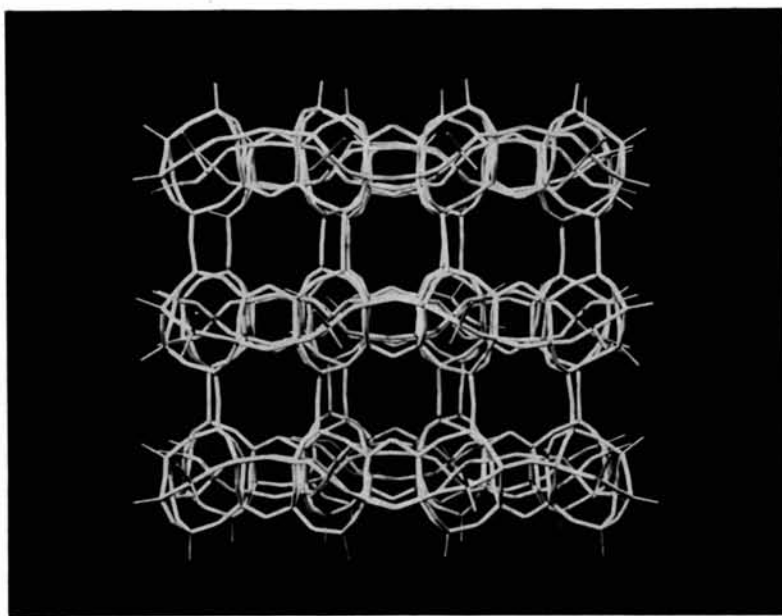


Fig. 2. Projection of the stilbite structure on the (010) plane. Numbers give the heights of the atoms in thousandths of the cell edge. Continuous lines are Si-O bonds; dashed lines are cation-water (or oxygen) bonds.



(a)



(b)

Fig. 1. Stereographic view of the stilbite framework viewed (a) along a and (b) along the $[102]$ axis.

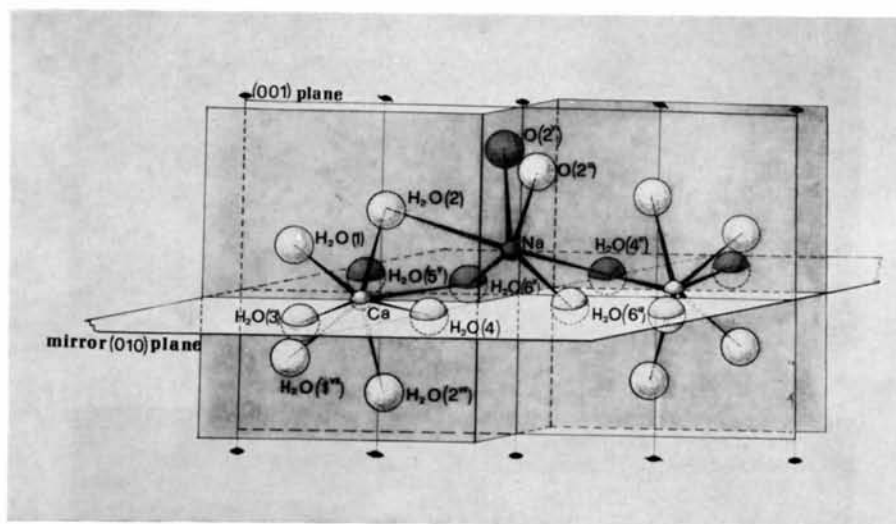


Fig. 3. Assonometric view of the Ca-8H₂O spheroids lying on the mirror (010) plane. A sodium atom is also shown; it coordinates four water molecules and two framework oxygen atoms which are the two highest anions in the Figure. Although the sodium is near the twofold axis, only one atom is shown because of its low (22%) statistical occupancy.

Table 5 (*cont.*)

Ca-All oxygens ≥ 4.22	
Na polyhedron	
Na-O(2 ⁱⁱⁱ)	2.46 \pm 0.04
Na-O(2 ^v)	2.63 \pm 0.04
Na-H ₂ O(2)	3.07 \pm 0.05
Na-H ₂ O(4)	2.53 \pm 0.05
Na-H ₂ O(4 ⁱⁱ)	3.25 \pm 0.05
Na-H ₂ O(6 ⁱⁱⁱ)	2.25 \pm 0.06
Na-H ₂ O(6 ^v)	2.25 \pm 0.06

Essentially there is a spheroidal hydrated Ca-8H₂O group as shown in Fig. 3. The Ca-H₂O distances are listed in Table 5. Seven distances fall in a narrow range (from 2.38 Å to 2.51 Å), the eight Ca-H₂O distance is a little larger than the preceding ones (2.70 Å). The biggest channels surrounded by ten-tetrahedra rings are filled by Ca-8H₂O spheroids. Between these spheroids and channel walls there are cavities; sodium atoms occupy these sites statistically; in reality these positions are occupied by a lesser amount of other exchangeable cations such as Ca and Mg, which, of course, are statistically distributed over these sites too. These positions are surrounded by three water molecules and two framework oxygen atoms, if atoms at a distance of more than 3 Å are neglected. The five Na-O, H₂O distances vary from 2.25 to 2.63 Å, in close

agreement with the lengths given in the literature; two more distances of 3.07 and 3.25 Å respectively seem too large to be considered here. Therefore the coordination number of sodium atoms, excluding the two largest distances, can be taken as five and the coordination polyhedron can be described as a tetragonal pyramid parallel to the [101] direction, sharply skewed to one side.

Not all water molecules sites are completely filled; occupancy factors from 80 to 90 % may occur. Table 6 lists all distances less than 3.65 Å between water molecules, and between water molecules and framework oxygen atoms. The coordination of the water molecules in stilbite are complex and varied, which is not surprising in view of the patterns found in other zeolites.

It is not really possible to draw a line between bonded and non-bonded neighbours for distances larger than 3 Å. As the value of 3.01 Å is taken as the largest distance from close neighbours it may be seen that the coordination around water molecules varies from triangular to octahedral as shown in Table 6.

The H₂O(1) and H₂O(3) molecules are surrounded by four neighbouring water molecules, the H₂O(4) and H₂O(2) by three and two water molecules respectively, while H₂O(5) and H₂O(6) are linked only to one water molecule. All water molecules are bonded to one framework oxygen atom, except H₂O(4) and H₂O(6) which

Table 6. Distances less than 3.65 Å related to water molecules

Interatomic distances symmetrically equivalent are bracketed.				
H ₂ O(1) polyhedron		Distances		
H ₂ O(1)-H ₂ O(1 ⁱ)	2.90 \pm 0.06 Å	H ₂ O(3)-H ₂ O(3 ^{viii})	3.01 \pm 0.05 Å	
H ₂ O(1)-H ₂ O(1 ^{vii})	2.83 \pm 0.05	H ₂ O(3)-H ₂ O(4)	2.92 \pm 0.05	
H ₂ O(1)-H ₂ O(2)	2.85 \pm 0.03	H ₂ O(3)-O(8)	2.99 \pm 0.02	
H ₂ O(1)-H ₂ O(3)	3.01 \pm 0.04	H ₂ O(3)-O(9)	3.61 \pm 0.03	
H ₂ O(1)-H ₂ O(5 ^v)	3.10 \pm 0.04	H ₂ O(3)-O(10 ⁱⁱⁱⁱ)	3.11 \pm 0.02	
H ₂ O(1)-O(1 ^{iv})	3.23 \pm 0.03	H ₂ O(4) polyhedron		
H ₂ O(1)-O(1 ^v)	2.93 \pm 0.03	H ₂ O(4)-H ₂ O(2)	} 3.01 \pm 0.03	
H ₂ O(1)-O(4)	3.22 \pm 0.03	H ₂ O(4)-H ₂ O(2 ^{vii})		
H ₂ O(1)-O(5)	3.54 \pm 0.03	H ₂ O(4)-H ₂ O(3)	2.92 \pm 0.05	
H ₂ O(1)-O(8)	3.58 \pm 0.03	H ₂ O(4)-H ₂ O(6 ^v)	3.07 \pm 0.06	
		H ₂ O(4)-H ₂ O(6 ^{vi})	3.35 \pm 0.06	
H ₂ O(2) polyhedron		H ₂ O(5) polyhedron		
H ₂ O(2)-H ₂ O(1)	2.85 \pm 0.03	H ₂ O(5)-H ₂ O(1 ^v)	} 3.10 \pm 0.04	
H ₂ O(2)-H ₂ O(3)	3.44 \pm 0.03	H ₂ O(5)-H ₂ O(1 ^{ix})		
H ₂ O(2)-H ₂ O(4)	3.01 \pm 0.03	H ₂ O(5)-H ₂ O(2)	} 3.55 \pm 0.03	
H ₂ O(2)-H ₂ O(5)	3.55 \pm 0.03	H ₂ O(5)-H ₂ O(2 ^{ix})		
H ₂ O(2)-H ₂ O(6 ^v)	3.25 \pm 0.04	H ₂ O(5)-H ₂ O(6)	2.80 \pm 0.05	
H ₂ O(2)-O(1)	3.59 \pm 0.02	H ₂ O(5)-O(4 ⁱⁱⁱ)	2.82 \pm 0.02	
H ₂ O(2)-O(1 ^v)	3.54 \pm 0.03	H ₂ O(5)-O(7)	3.52 \pm 0.01	
H ₂ O(2)-O(2 ^v)	3.16 \pm 0.02	H ₂ O(6) polyhedron		
H ₂ O(2)-O(5)	3.63 \pm 0.02	H ₂ O(6)-H ₂ O(2 ^v)	} 3.25 \pm 0.04	
H ₂ O(2)-O(7)	3.60 \pm 0.02	H ₂ O(6)-H ₂ O(2 ^{ix})		
H ₂ O(2)-O(7 ^v)	2.82 \pm 0.02	H ₂ O(6)-H ₂ O(4 ^v)	3.07 \pm 0.06	
H ₂ O(2)-O(10)	3.60 \pm 0.02	H ₂ O(6)-H ₂ O(4 ^{iv})	3.35 \pm 0.06	
H ₂ O(3) polyhedron		H ₂ O(6)-H ₂ O(5)	2.80 \pm 0.05	
H ₂ O(3)-H ₂ O(1)	} 3.01 \pm 0.04	H ₂ O(6)-O(2)	3.46 \pm 0.02	
H ₂ O(3)-H ₂ O(1 ^{vii})		} 3.44 \pm 0.03	H ₂ O(6)-O(6)	3.24 \pm 0.03
H ₂ O(3)-H ₂ O(2)				
H ₂ O(3)-H ₂ O(2 ^{viii})				

have bond lengths not less than 3.24 Å with the framework oxygen atoms. Only these two water molecules are contemporaneously bonded either to Ca or Na atoms.

Increasing the limit suggested above to 3.65 Å, the coordinations obviously become larger and more complex. The arrangement of water molecules in the specimen of stilbite used for this investigation does not confirm the Gabuda *et al.* (1963) hypothesis. In their specimen the above workers found that in the temperature range -60 to $+150^{\circ}\text{C}$ the water molecules are grouped in pairs with a distance of 2.74 ± 0.15 Å and that the distances between different pairs of molecules are considerably larger than the distances between the grouped molecules. As can be seen from Table 6 this hypothesis has not been confirmed with the specimen used for this investigation, the range of the water-water distances within each possible pair and between the different pairs being too close to satisfy it.

Cleavage

The (010) cleavage of stilbite is very good and can readily be explained on consideration of Fig. 1(a) and (b). The planes $y/b=0, \frac{1}{2}$ cut a minimum number of Si-O-Si bonds. The values of 1.7 bonds per 100 Å² is the lowest found in zeolite structures (Meier, 1968). Moreover, the perfect cleavage must be related also to the very small number of bonds between the exchangeable cations and framework oxygen atoms.

The lamellar habit of stilbite can, of course, also be explained in a similar way.

Twinning

Stilbite crystals exhibit complex twins which show components with four different orientations, and also zones with fine sheaf-like intergrowth of uncertain significance [see Fig. 4(a)]. Bearing in mind that:

- stilbite is pseudo-orthorhombic,
 - the morphology of the twins is the same as the un-twinned crystals,
 - the orientation of the optical indicatrix is almost the same in all components of the twins,
- one can conclude for a pseudosymmetry twinning: the tetrahedral framework continues throughout the twins with only a slight distortion, so that in the different part the *a* direction is the same, and the [101] and *c* direction are interchanged, as shown in Fig. 4(b). As the sum of the different angles around the centre is no longer 180° [see Fig. 4(c)], a sheaf-like aggregate is necessary to 'close' the angle to 180°.

Relationship with other zeolites

It is not difficult to place stilbite in the heulandite group, because of the presence in its framework of rings of 4, 5, 6 and 8 tetrahedra and of the common presence of the characteristic polyhedral configuration

quoted above. The exchangeable cations environment, however, is partially different.

If in all zeolites of this group the cations are situated within the cavities formed by intersecting channels, stilbite is the first zeolite in which a type of cation site is completely insulated from direct contact with the framework by a sphere of hydration. An example of this type has been said to occur only in levinite where a cation position has been found to be coordinated by 9 water atoms (Kerr & Williams, 1969). A similar coordination also occurs in chabazite where the calcium is surrounded by six water molecules and by one framework oxygen atom (Smith, Rinaldi & Dent Glasser, 1963). In stilbite a second type of cation position is

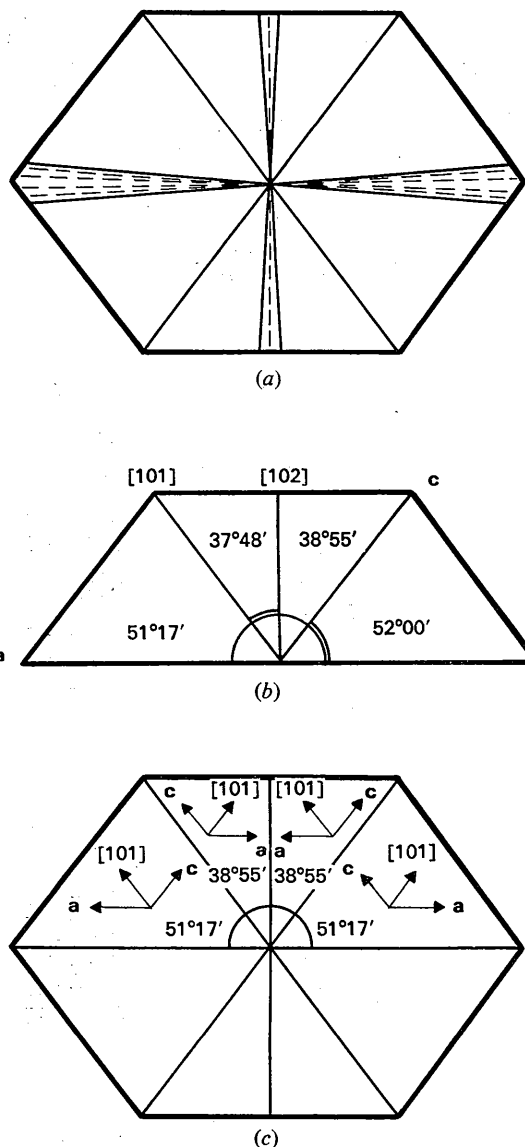


Fig. 4. (a) Schematic drawing of a stilbite twin; (b) angular values emphasizing the pseudo ortho-rhombicity of stilbite; (c) proposed interpretation of the twins shown in (a).

present; it is occupied only on a statistical basis (occupancy of 22%) by sodium atoms. This cation could be said to be attached to the cavity wall, while the surface still exposed is coordinated by water molecules. This type of coordination is usual in zeolites and has been found, for instance in harmotome (Sadanaga, Marumo & Takéuchi, 1961), jugawaralite, and has also been noted in gismondite and levinite (Kerr & Williams, 1969).

Note added in proof: Since the acceptance of this paper another study on the refinement of stilbite has been published (Slaughter, 1970). Differences between the two papers are slight: Slaughter examines cation positions < 5% occupancy; he suggests a different interpretation of the distribution of Si/Al atoms; temperature factors are slightly different.

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The Crystal Structure of L-Dopa Hydrochloride, 3-(3,4-Dihydroxyphenyl)-L-Alanine Hydrochloride, C₉H₁₂O₄NCl*

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The crystal structure of L-dopa hydrochloride, 3-(3,4-dihydroxyphenyl)-L-alanine hydrochloride, was determined from three-dimensional data collected manually with a General Electric XRD6 diffractometer using Cu $K\alpha$ radiation. The crystals are monoclinic, $P2_1$, with $a = 6.261 \pm 0.007$, $b = 5.821 \pm 0.001$, $c = 15.646 \pm 0.003$ Å, and $\beta = 112.66 \pm 0.02^\circ$. The structure was refined to a conventional R value of 7.9%. Extensive intermolecular hydrogen bonding is present. The aromatic ring forms an angle of 39.1° with the plane of the carboxyl group.

The compound 3-(3,4-dihydroxyphenyl)-L-alanine (L-dopa) (Fig. 1) has been used for the treatment of Parkinson's disease. Slowly increasing oral doses of L-dopa have been reported to induce at least partial improvement of some of the manifestations of Parkinson's disease, and in some cases the improvement has been

dramatic (Cotzias, Papvasiliou & Gellene, 1969). Because of the interest in this compound as a promising therapeutic agent, the study of the crystal structure of the hydrochloride of this amino acid was undertaken.

Experimental

Crystals of the hydrochloride of L-dopa were obtained by the evaporation of a solution of L-dopa in concentrated hydrochloric acid. The L-dopa was obtained from Nutritional Biochemicals Corporation. The crystal was aligned with the unique b axis parallel to the φ axis of a General Electric XRD6 diffractometer single-crystal orienter. The space group was determined to be $P2_1$ by searching for reflections with the diffracto-

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